Traffic light control based on Fuzzy Q-learning

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Abstract—Traffic is an issue that many big cities are confronted with because of ever-increasing population growth. In this paper we propose a two phase traffic light control system based on fuzzy Q-learning for an isolated 4-way intersection. The states and actions of the Q-learning variables is set by a fuzzy algorithm which can be learned through environmental interactions and taking advantage of fuzzy logic. The proposed algorithm was simulated for a period of one hour for each of 14 different traffic conditions. Comparison with other methods was carried out on the 14 traffic conditions. The results showed that the proposed algorithms decrease the total waiting time and the mean of queue length.

Index Terms—Fuzzy logic, fuzzy Q-learning, traffic light control.

I. INTRODUCTION

Many big cities are confronted with heavy traffic because of the ever-increasing population growth. Efficient methods for traffic flow management are necessary to optimize the use of available road capacity. Furthermore, high fuel prices and environmental problems are other important reasons to reduce traffic. Therefore, the need arise for simulating and optimizing traffic control system that can adapt with this increasing congestion. We tried to decrease traffic congestion through the development of an intelligent traffic control system, which is based on the traffic density flow at the intersection. Many research activities have attempted to solve different traffic problems in the intelligent transportation system [1,2,3,4,5]. In many cases, a fixed time traffic light control system has been used with the aim of minimizing waiting time and the number of vehicles waiting at intersections. However, it is of interest to apply dynamic traffic light control systems in which green light duration is adjusted to environmental dynamic changes to maximize throughput and minimize the waiting time. Fuzzy control systems use fuzzy logic, which can simulate human intelligence to control traffic and enable implementation of real world rules and human-like thinking process. Fuzzy control is an approach that can be applied to various traffic models. The fuzzy logic traffic light controllers utilize sensors to count the number of vehicles. Therefore, the resulting controllers control the traffic lights according to traffic density [6]. There are different approaches to control traffic lights based on artificial intelligence methods such as fuzzy logic, neural networks, reinforcement learning and evolutionary algorithms. These methods can lead to shorter queues and less traffic delay.

Many studies have focused on intelligent traffic light control. There are two approaches for traffic light control, including pre-timed [7] and sensor-based signal controls. The preset cycle time methods present the traditional strategy and consist of a preset interval series which cannot respond to unpredictable conditions and waste of time for less congested roads [8]. The vehicle actuated methods are sensor based methods in which the green light time can be extended based on demand.

To overcome the mentioned problems and in order to reduce the waiting time and the queue length, we proposed a Q-learning fuzzy controller which is based on the traffic density. As this paper considers the traffic light control approach, the existing methods in this category are briefly discussed below.

Smith et al. proposed a neural network based approach for traffic light control. This approach has a time consuming learning process and reduces waiting time by 10% [9]. The use of fuzzy logic provides a high quality performance approach to control the traffic congestion [10,11]. Arora et al. measured traffic density on the road using morphological edge detection and a fuzzy logic technique [12].

Tari et al. used a two level hierarchical fuzzy rule-based system for controlling complex traffic intersection [13]. Keyparslan et al. used computer vision techniques and neural networks to extract the traffic data and applied a fuzzy ontology to control traffic light in isolated intersection [6]. Shakeri et al. introduced a three layer fuzzy system based on the cellular automata for optimizing traffic light control [14].

Abdulhai et al. provide an isolated traffic signal controller using reinforcement learning which could combine with dynamic route guidance [15]. Also multi-agent Q-learning was used for a non-stationary environment that estimated states based on the average queue length [16].

In order to minimizing the waiting time of the public transportation and reducing the computational complexity, dynamic programming and branch-and-bound techniques were combined to control traffic lights [17].

Liu et al. presented a differential evolution bacteria foraging optimization algorithm to minimize the delay vehicles of a cycle time, and also maximize throughput of the intersection [18]. In another work, vehicles were detected by the Prewitt edge detector and image matching and the traffic light duration was determined based on the percentage of matching [19].

Dujardin et al. applied mixed integer linear programming (MILP) for multimodal traffic light control based on optimization of three criteria including the total delay of
In this paper, we propose a two phases real-time approach based on fuzzy Q-learning for adjusting traffic light duration for an isolated intersection based on traffic flow. Compared to pre-set cycle time (PCT) and vehicle actuated (VA) approaches, the proposed method can reduce the average number of vehicles in traffic queues and the average waiting time for vehicles. The proposed system can learn the various relationships between traffic conditions and the optimal actions using its experience in different situations. Furthermore, it can effectively work in specific situations based on its past experience with the same or similar situations.

The advantages of the proposed approaches are as follows:

- No need to pre-specified models, and training possible for any traffic conditions.
- Can learn the relationships between states and actions using environmental interactions.
- Benefit from the fuzzy system advantages.

The rest of this paper is organized as follows. Section 2 reviews fuzzy Q-learning and presents the algorithm scheme. Section 3 reports experimental results and section 4 concludes the paper.

II. PROPOSED METHOD

The proposed method is shown in Fig. 1. Q-learning has been used for learning fuzzy systems [21]. Since the state and actions of Q-learning algorithm can be set by fuzzy variables, Q-learning can take advantage of fuzziness.

In this paper, a fuzzy Q-learning controller is designed for an isolated 4-way traffic intersection. The Q-learning information is used in tuning the output membership functions of the fuzzy controller. Before the end of each phase, the next green optimum phase durations estimated based on current traffic conditions which are specified by four variables include in the number of vehicles in the north, the south, the east and the west which are shown by $q_l_{north}$, $q_l_{south}$, $q_l_{east}$, $q_l_{west}$, respectively. Two input variables are considered for the traffic lights control:

- $Max_{ql_{ns}}$: the maximum number of vehicles in the north-south and the south-north ($max (q_l_{north}, q_l_{south})$)
- $Max_{ql_{ew}}$: the maximum number of vehicles in the east-west and west-east ($max (q_l_{east}, q_l_{west})$)

The green light and red light specified the arrival side and queue side, respectively. The proposed algorithm determined the optimal next phase duration for the queue side based on the current queue lengths. The north-south and east-west Q-tables are used where size is determined as:

$$ Q_{table – size} = noas \times noqs \times NAction $$

where $noas$ is the number of the arrival side membership functions and $noqs$ is the number of the queue side membership functions, and $NAction$ is the number of actions.

![Figure 1. Fuzzy Q-Learning Traffic Light Control Schematic.](archive-of-sid.ir)
The proposed algorithm is described as follows:
1. Based on the number of vehicles in each queue, the variables Max_ql_ns and Max_ql_ew are calculated as an input for the next step of the algorithm.
2. Four fuzzy sets are defined on each dimension of the two dimensional state space, $m_{i1}^{f1}$ and $m_{i2}^{f2}$ are the corresponding membership function in which $i \in \{\text{low, medium, high, very high}\}$ as are illustrated in Fig. 2. Each rule is associated with a set of possible discrete actions $Act_{i1,i2} = \{ \text{act}_{i1,i2,r_1}, \text{act}_{i1,i2,r_2}, \ldots, \text{act}_{i1,i2,r_k} \}$

where $j_1, j_2 = 1, 2, \ldots, k$, show the number of membership functions, and $r = 1, 2, \ldots, u_R$ where $u_R$ is the number of rules. The corresponding action values are defined as follow:

$$Q_{i1,i2} = \{q_{i1,i2,r_1}, q_{i1,i2,r_2}, \ldots, q_{i1,i2,r_k} \} \quad (2)$$

According to the above definitions, the generic rule $R_r$ may be written as follows:

$$R_r : \text{If Max}_q_{\text{ql}}_{\text{ns}} \text{is } m_{i1}^{f1} \text{ and Max}_q_{\text{ql}}_{\text{ew}} \text{ is } m_{i2}^{f2} \text{ then output } = a_{r,1} \text{ with } q_{r,1} \text{ OR } a_{r,2} \text{ with } q_{r,2} \text{ OR } \ldots \text{ OR } a_{r,u_R} \text{ with } q_{r,u_R}$$

When Max_ql_ns and Max_ql_ew enter the system, they are fuzzified based on the membership function. All of the rules are activated partially by a certain activation level which is calculated as follow:

$$\varphi_r = \mu_{i1}^{f1}(\text{Max}_q_{\text{ql}}_{\text{ns}}) \ast \mu_{i2}^{f2}(\text{Max}_q_{\text{ql}}_{\text{ew}}) \quad (3)$$

where $\mu_{i1}$ and $\mu_{i2}$ are truth degrees.
3. Since each input variable belongs to several fuzzy sets with different activation levels, the activation level is normalized and is considered as the weight of each of the winning actions of rule:

$$\varphi_{\text{norm}} = \frac{\varphi_r}{\sum_{r=1}^{u_R} \varphi_r} \quad (4)$$

4. The time of green light is calculated based on the average weight method:

$$Act = \sum_{r=1}^{u_R} \varphi_r \ast win\_act_r \quad (5)$$

where $\varphi_r$ and $win\_act_r$ are the weight and winning action of the $r^{th}$ rule, respectively.

5. After the calculation of the next green light duration, the output value which is between -1 and 1, is mapped to the original range. In this paper, the original range is multiples of 5 between 10 and 100.
6. After each phases, the punishment is calculated based on the queue length variation.

$$\text{Punishment} = \sum_{i=1}^{u_R} \{ \max (|q_{i1}^{\text{new}} - q_{i1}^{\text{old}}|, 1) \ast \text{sgn}(q_{i1}^{\text{new}} - q_{i1}^{\text{old}}) \} \quad (6)$$

where $q_i \in \{q_{\text{north}}, q_{\text{south}}, q_{\text{east}}, q_{\text{west}}\}$
7. After calculating the punishment, the arrival side Q table is updated. Gradient descent is usually used to update the parameters of algorithm:

$$q_{r+1} = q_r - \alpha \epsilon \Psi_r \quad (7)$$

where $\gamma$ is discount factor and $\alpha$ is learning rate.
8. The above steps are done for each of the 14 different traffic conditions in one hour simulations and then are repeated until convergence.

![Figure 2. The membership functions for arrival side and queue side.](image-url)
Table 1. Intersection traffic conditions [22]

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<tr>
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<td>0.75</td>
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Table 2. The mean of total waiting and mean of q length of different algorithms.

<table>
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<tr>
<th>Traffic Condition</th>
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<th>VA</th>
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Figure 3. The mean total waiting time
Figure 4. The mean of queue length

B. Experimental Results

In this section, we present the results of our experiments. We assessed and compared the proposed algorithm with two other traffic light control methods, namely PCT and VA on the 14 traffic conditions. Based on the arrival and departure time of each vehicle, the total waiting time and mean queue length are calculated.

The mean of total waiting time (MTW) and mean of queue lengths (MQL) are calculated for each algorithm in Table 2.
According to table 2, the mean of queue length and mean of total waiting time of the results are nearly similar in the light, and moderate traffic condition which are colored in black. The important case appears in the heavy traffic conditions. Our algorithm achieves a better result than the other algorithms, especially in unbalanced traffic conditions, where the input rate of one side is heavy and other methods show critical results.

The mean total waiting time of the three algorithms are compared in Fig. 3. PCT and VA face difficulties in the more unbalanced condition and heavier input rate. However the proposed algorithm achieves better results and can deal with such conditions. The comparison of the mean of queue length of three algorithms is illustrated in Fig. 4.

In asymmetrical traffic increase from different directions, the fuzzy Q-learning controls traffic in shorten mean queue length and total waiting time.

IV. CONCLUSIONS

We proposed a two phase traffic light control system based on fuzzy Q-learning for an isolated 4-way intersection. A fuzzy algorithm set the Q-learning variables. The proposed algorithm benefits from fuzzy system advantages and can learn the fuzzy rules using environmental interactions. Before the end of each phase, the next green optimum phase durations estimated based on current traffic conditions which are specified. This algorithm was compared with two other algorithms, namely VA and PCT for a period of one hour for each of 14 different traffic conditions. As shown in the results, the proposed algorithm outperformed the other algorithms significantly in heavy traffic and unbalanced traffic conditions, whereas in other situations the three algorithms were similar.

REFERENCES